

Eindexamen wiskunde B1 vwo 2002-I

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Verschuivend zwaartepunt

$$1. \quad d_T = \frac{3}{3+10} \cdot \frac{1}{2} \cdot 3 + \frac{10}{3+10} \cdot 5 \text{ cm} = 4,2 \text{ cm}$$

$$2. \quad d_T = \frac{h}{h+10} \cdot \frac{1}{2} \cdot h + \frac{10}{h+10} \cdot 5 = \frac{\frac{1}{2} \cdot h^2}{h+10} + \frac{50}{h+10} = \frac{h^2}{2h+20} + \frac{100}{2h+20} = \frac{h^2+100}{2h+20}$$

$$3. \quad \frac{h^2+100}{2h+20} = 4,5 \quad h^2 - 9h + 10 = 0$$

$$h = \frac{9 \pm \sqrt{81-40}}{2} \Rightarrow h = 4\frac{1}{2} - \frac{1}{2}\sqrt{41} \quad \vee \quad h = 4\frac{1}{2} + \frac{1}{2}\sqrt{41}$$

$$\frac{h^2+100}{2h+20} - 4,5 < 0 \quad \begin{array}{c} + \qquad \qquad - \qquad \qquad + \\ \hline \qquad \qquad 1,3 \qquad \qquad 7,7 \end{array}$$

$$d_T < 4,5 \quad 1,3 < h < 7,7$$

$$4. \quad d_T' = \frac{2h(2h+20) - 2(h^2+100)}{(2h+20)^2} = \frac{2h^2+40h-200}{(2h+20)^2}$$

$$d_T' = 0 \quad h^2 + 20h - 100 = 0 \quad \wedge \quad (2h+20)^2 \neq 0$$

$$h = \frac{-20 \pm \sqrt{400+400}}{2} \Rightarrow h = -10 - \sqrt{200} \quad \vee \quad h = -10 + \sqrt{200}$$

$$\text{Minimale afstand} \quad h = -10 + \sqrt{200}$$