

Snijden en schuiven

8. $A_V = \int (g(x) - f(x)) dx$

$$f(x) = g(x) \quad \rightarrow \quad x^2 = 3\sqrt{x}$$

$$\rightarrow \quad x = 0 \quad \text{of} \quad x = \sqrt[3]{9} = 3^{\frac{2}{3}}$$

$$A_V = \int_0^{3^{\frac{2}{3}}} (3\sqrt{x} - x^2) dx = \left[2x^{\frac{3}{2}} - \frac{1}{3}x^3 \right]_0^{3^{\frac{2}{3}}} = 6 - 3 = 3$$

9. $g(a) = 2 \cdot f(a)$

$$3\sqrt{a} = 2 \cdot a^2 \quad \rightarrow \quad 9 \cdot a = 4 \cdot a^4 \quad \rightarrow \quad a = 0 \quad \text{of} \quad 4a^3 = 9$$

$$\text{Dus } AB = BC \text{ geldt voor } a = \left(\frac{9}{4}\right)^{\frac{1}{3}} = \left(\frac{3}{2}\right)^{\frac{2}{3}}$$

10. Er moet gelden: $f'(x) = g'(x)$

$$2x = \frac{3}{2\sqrt{x}} \quad \rightarrow \quad 4x^{3/2} = 3 \quad \rightarrow \quad x = \left(\frac{3}{4}\right)^{\frac{2}{3}}$$

$$\text{De grafiek is } g\left(\left(\frac{3}{4}\right)^{\frac{2}{3}}\right) - f\left(\left(\frac{3}{4}\right)^{\frac{2}{3}}\right) = 2,726 - 0,681 = 2,04 \text{ omhoog geschoven.}$$