

Gebroken functie

$$4. \quad f'(x) = 1 - \frac{4}{x^2} = 0 \rightarrow x^2 = 4 \rightarrow x = -2 \quad \vee \quad x = 2$$

De toppen zijn $(-2, f(-2))$ en $(2, f(2))$ dus
 $(-2, -4)$ en $(2, 4)$

$$5. \quad y = f(x) \rightarrow x + \frac{4}{x} = 5 \rightarrow (x-1) \cdot (x-4) = 0 \rightarrow x = 1 \quad \vee \quad x = 4$$

$$A_v = 3 \cdot 5 - \int_1^4 \left(x + \frac{4}{x}\right) dx = 15 - \left[\frac{1}{2}x^2 + 4 \ln x\right]_1^4 = 15 - (8 + 4 \ln 4 - \frac{1}{2}) = 7\frac{1}{2} - 4 \ln 4$$

$$6. \quad L_{v_1} = \int_1^4 \sqrt{1 + (f'(x))^2} dx = \int_1^4 \sqrt{1 + \left(1 - \frac{4}{x^2}\right)^2} dx = 3,79$$

Met de GR: $y_1 = \sqrt{1 + (1 - 4/x^2)^2}$

Optie $\int f(x) dx$ linkergrens 1 rechtergrens 4 uitkomst 3,79

$$L_{v_2} = 4 - 1 = 3 \rightarrow L_v = 3 + 3,79 = 6,79$$